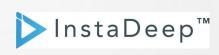
Keep the Gradients Flowing: Using Gradient Flow to Study Sparse Network Optimization

Kale-ab Tessera, Sara Hooker, Benjamin Rosman









Deep Learning: Key Challenges

Problems with overparameterization:

- → Higher cost of training time, compute etc.
- → Increase the latency and memory footprint.
- → Overparameterized networks are more prone to memorization.

Renewed focus on compression techniques -> sparsity/pruning.

Why is Sparsity Interesting?

Sparse Networks can lead to:

- **Gaster training and inference times.** [1,2,3]
- □ More robust to noise. [4]
- □ Improving efficiency memory or energy. [5,6]

Similar or better performance than dense networks?

Types of Sparsity

1. Sparse Activity

Only fraction of neurons are active -> Sparse Neurons.

2. Sparse Connectivity

Neurons are only connected to only a subset of neurons in the previous layer -> Sparse Weights.

Sparsity Research - Focus on Initialization

- A lot of great work focusing on initialization - finding special weight initializations or "lottery tickets". [7,8,9]
- Focusing on initialization alone has proved to be inadequate. [10,11]
- Optimization outside of early stages of training is poorly understood - e.g. sensitivity of lottery tickets to higher learning rates. [9,10,11]

- Existing work:
 - Grad Flow during DST [12]
 - Loss landscape [13]
 - Signal propagation [14]
 - SGD Noise [15]
- What about training dynamics?
 - Regularization/ Normalization.
 - Optimization methods.
 - Activation functions.
 - ➤ Learning rates.
 - > Their interactions?

Our Setting - When to Prune

- → Pruning Before Training (Pruning From Scratch)/Early in training.
- → <u>Pruning During Training (Dynamic Sparsity)</u>
- → <u>Pruning After Training</u>

Our Setting - What to Prune

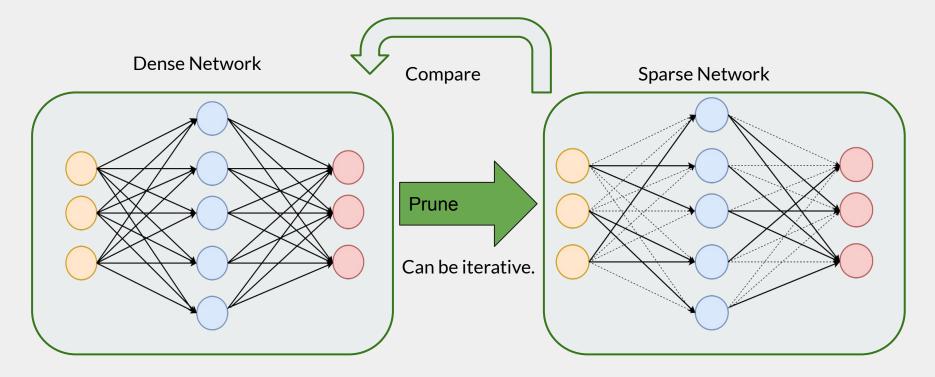
- Impact on loss or the Hessian of the loss function.
- Magnitude Pruning.
- Connection sensitivity/Salency SNIP[16] / SynFlow[17].
- Gradient flow GRASP[18].
- Random Pruning.

[11,19] showed that for pruning from scratch methods, shuffling the preserved weights does not affect final performance.

Sparsity Setting

Pruning From Scratch + Random Pruning.

Current way to compare sparse and dense networks



Issues

- 1. Networks are **different capacity**.
- 2. Initial weight distributions are different.
- 3. Training times are different.

Ensure Same Capacity

Goal: Ensure same number of nonzero weights in Sparse and Dense networks.

Sparse Networks **S**, Dense Network **D**, **Q**^{I} is the weights in layer I and **m**^{I} is the mask applied to layer I.

$$a_{S}^{l}= heta_{S}^{l}\odot m^{l}$$
 , $a_{D}^{l}= heta_{D}^{l}$, for l

 $l=1,\ldots,L$,

Active weights in layer l of sparse network.

Active weights in layer l of dense network.

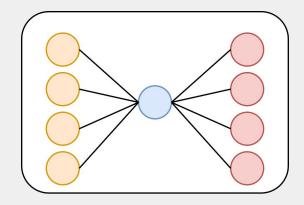
Ensure same number of nonzero weights in each layer for **S** and **D**.

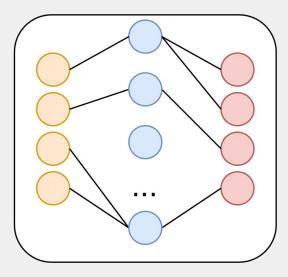
$$||a_S^l||_0 = ||a_D^l||_0, \quad ext{ for } \quad l=1,\ldots,L$$

Ensure Same Capacity

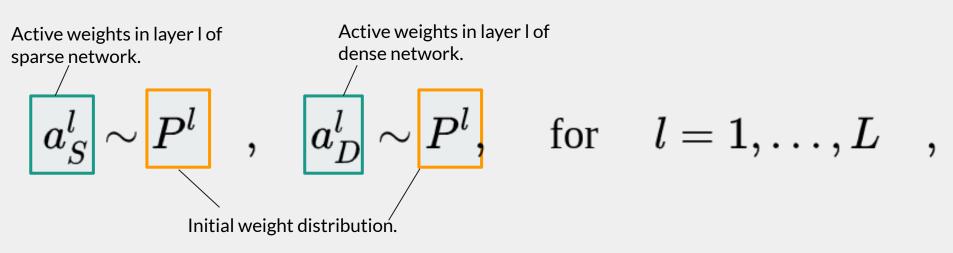
Dense Network

Sparse Network





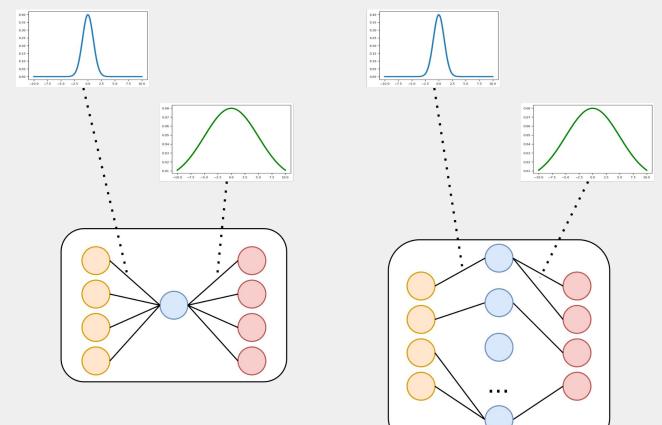
Same Initial Dist



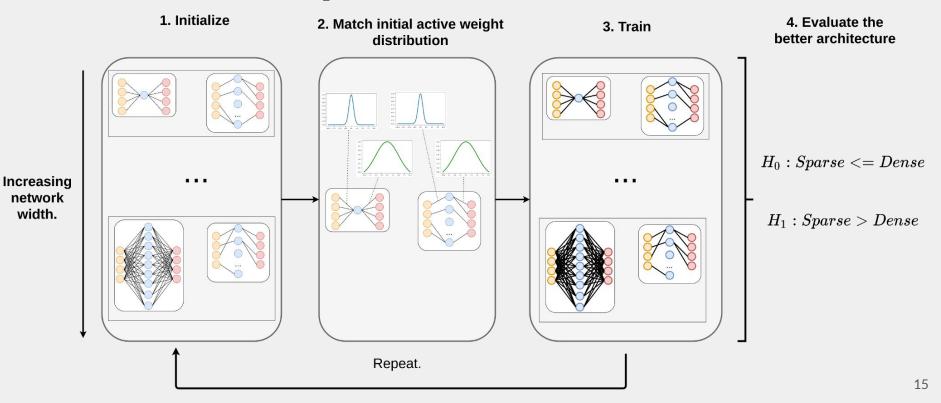
This is done by using a normal (or uniform) distribution, with

- Same mean (e.g. 0 in He Init) and
- Scaling the variance of the sparse network (fan-ins/fan-outs) to the same variance as its equivalent dense network.

Same Initial Dist



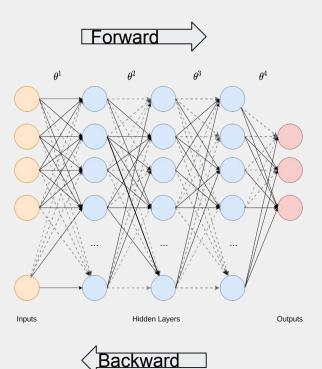
Same Capacity Sparse vs Dense **Comparison (SC-SDC)**



width.

Gradient Flow - Sparse networks.

- Historically, exploding and vanishing gradients were a common problem in neural networks.
- Exasperated issue in sparse networks. [12,18]
- Therefore useful analysis tool for studying sparse network optimization.



Intuition.

Standard Gradient Flow

- Gradient flow ≈ **norm of the gradients** of network.
- We consider a feedforward neural network: $f : \mathbb{R}^D \to \mathbb{R}$, with weights θ and cost function **C**.
- Concatenate all the gradients into a single vector:

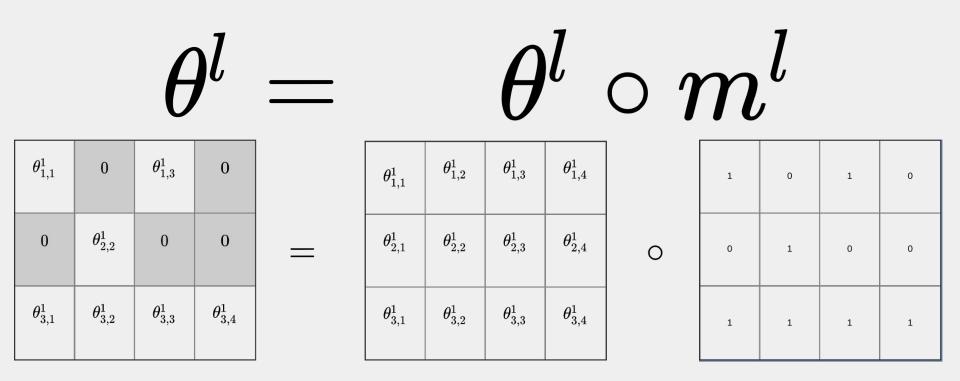
$$g=rac{\partial \mathcal{C}}{\partial heta}$$
- Take the pth-norm: $gf_p=||g||_p$

Example: L2 norm of gradients - gf_2

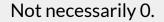
Issues

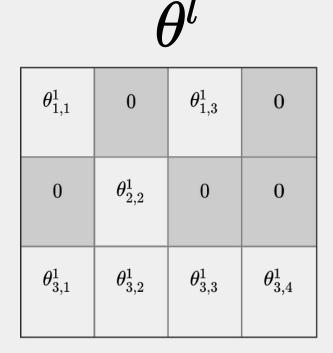
- 1. If you don't mask the gradients -> gradients of masked weights included in formulation.
- 2. Computing gradient norm by concatenating all the gradients into a single vector **gives disproportionate influence to layers with more weights.**

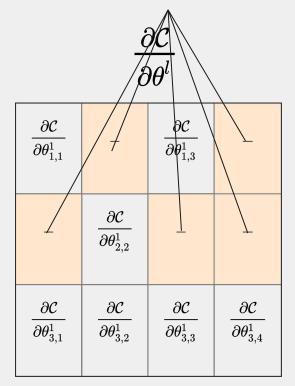
1. Masked Weights != Masked Gradients



1. Masked Weights != Masked Gradients







2. Disproportionate influence to layers with more weights.

Conv layer 32

ReLU+Pool Conv layer 64 Simple CNN ReLU+Pool Conv layer 64 ReLU+Pool Conv layer 128 ReLU+Pool Conv layer 128 ReLU+Pool Linear Layer

Linear Layer - Majority of the weights and -> disproportionate impact on gradient norm.

Effective Gradient Flow (EGF)

$$g = (rac{\partial \mathcal{C}}{\partial heta^1} \odot m^1, rac{\partial \mathcal{C}}{\partial heta^2} \odot m^2, \dots, rac{\partial \mathcal{C}}{\partial heta^L} \odot m^L)$$

$$EGF_p = rac{\sum\limits_{n=1}^{L}||g_n||_p}{L}$$

Compare GF -> EGF

- We train 600 MLPs for 500 epochs on Fashion-MNIST
- More than 10 000 MLPs for 1000 epochs on CIFAR-10 and CIFAR-100.

MLP - Correlation Between Gradient Flow Measures and Generalization Performance

	Measure	S	parse	Dense		
		Test Loss	Test Accuracy	Test Loss	Test Accuracy	
Н	$ g _1$	0.355	0.316	0.365	0.354	
\mathbf{IS}	$ \boldsymbol{g} _2$	0.282	0.292	0.285	0.329	
FMNIST	EGF_1	0.419	0.373	0.365	0.354	
FN	EGF_2	0.360	0.323	0.298	0.320	
CIFAR-10	$ \boldsymbol{g} _1$	0.440	0.327	0.380	0.251	
	$ \boldsymbol{g} _2$	0.447	0.308	0.355	0.290	
	EGF_1	0.371	0.300	0.380	0.252	
	EGF_2	0.451	0.332	0.363	0.287	
0	$ g _1$	0.355	0.385	0.325	0.319	
-10	$ \boldsymbol{g} _2$	0.373	0.393	0.357	0.385	
CIFAR-100	EGF_1	0.358	0.320	0.325	0.319	
	EGF_2	0.402	0.396	0.359	0.382	

*Lower bound - expect to see EGF >>> GF when used with CNNs.

Potential Use Cases for EGF

- More accurate analysis of sparse gradient flow.
- Possibility for Application in Gradient-based Pruning Methods
 - Gradient-based pruning methods like GRASP and SNIP have been to be susceptible to layer-collapse -> maybe EGF can help?

Results - SC-SDC and EGF

Configuration	Variants				
Optimizers	Adagrad, Adam, RMSProp, SGD and SGD with mom (0.9).				
Regularization/Normalization	No Regularization (NR), Weight Decay (L2), Data Augmentation (DA), Skip Connections (SC) and BatchNorm (BN).				
Number of hidden layers	1, 2 and 4.				
Dense Width	308, 923, 1538, 2153 and 2768.				
Activation functions	ReLU, PReLU, ELU, Swish, SReLU and Sigmoid.				
Learning rate	0.001 and 0.1.				
Datasets	Fashion-MNIST, CIFAR-10 and CIFAR-100.				

Results - EWMA vs Non-EWMA Optims

Non-EWMA Optims

Adagrad

SGD

SGD + mom (0.9)

EWMA (Exponentially weighted moving average) Optims

RMSProp

Adam

Results - Acronym

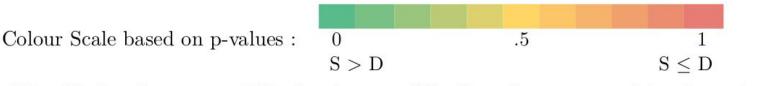
NR - No Regularization, BN - Batchnorm, SC - Skip Connections, DA - Data Augmentation, L2- weight decay, D - Dense Networks and S - Sparse Networks.

Average EGF - Average EGF calculated at the end of 11 epochs, evenly spread throughout the training.

E.g. 1000 epochs, this is calculated at the end of epoch 0, 99, 199, 299, 399, 499, 599, 699, 799, 899 and 999, and then compute the average.

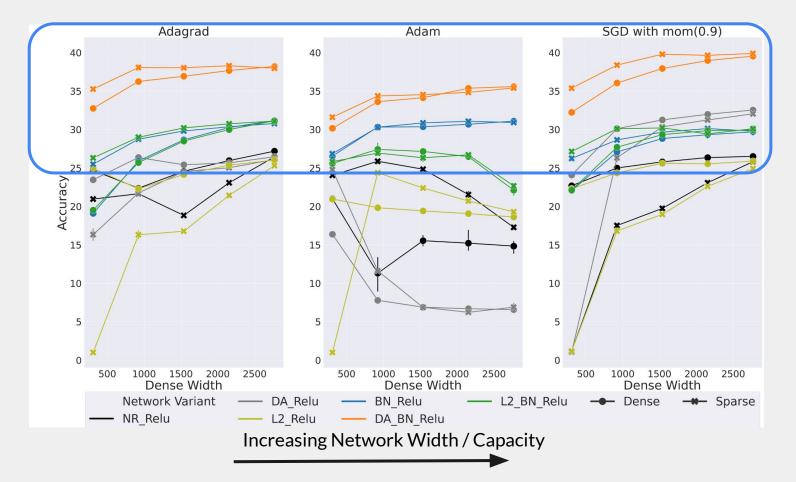
1. Batch Normalization Plays a Disproportionate Role in Stabilizing Sparse Networks

	NR	DA	L2	\mathbf{SC}	BN	DA_BN	$L2_BN$	SC_BN
Adagrad	1.000	1.000	0.998	0.239	0.006	0.002	0.001	0.003
Adam	0.000	0.055	0.198	0.003	0.079	0.051	0.254	0.166
RMSProp	0.001	0.000	0.300	0.166	0.117	0.021	0.914	0.541
SGD	1.000	1.000	1.000	0.248	0.000	0.000	0.001	0.003
Mom (0.9)	1.000	1.000	1.000	0.999	0.001	0.000	0.007	0.008

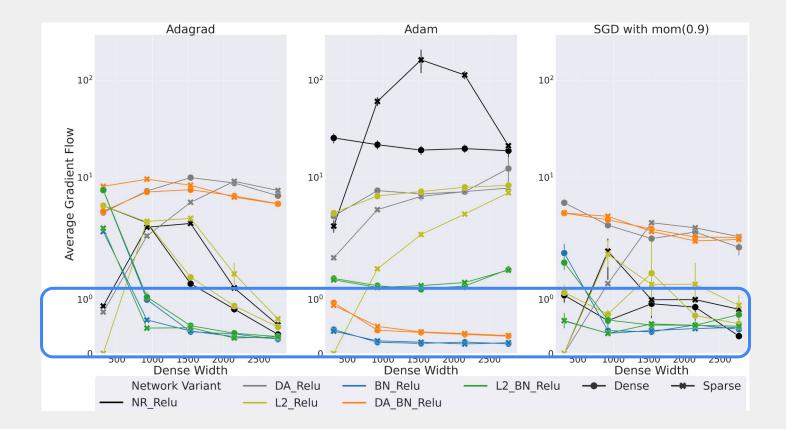


NR - No Regularization, BN - Batchnorm, SC - Skip Connections, DA - Data Augmentation, L2- weight decay, D - Dense Networks and S - Sparse Networks.

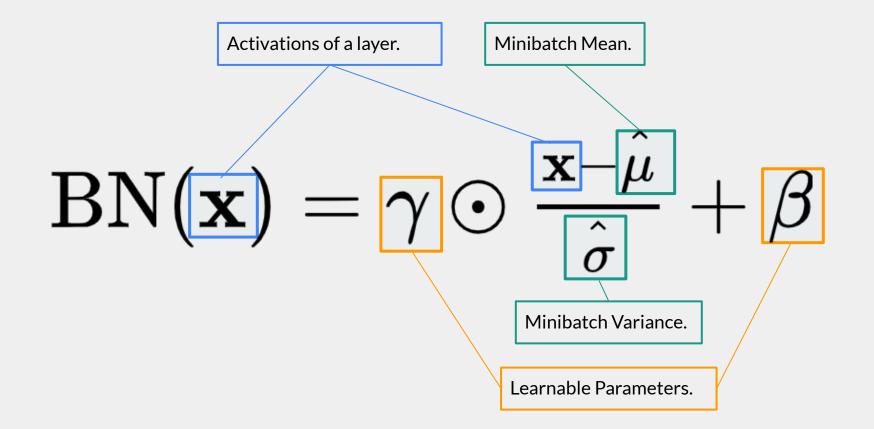
Batch Norm Stabilizes Grad Flow - Accuracy - 4hl



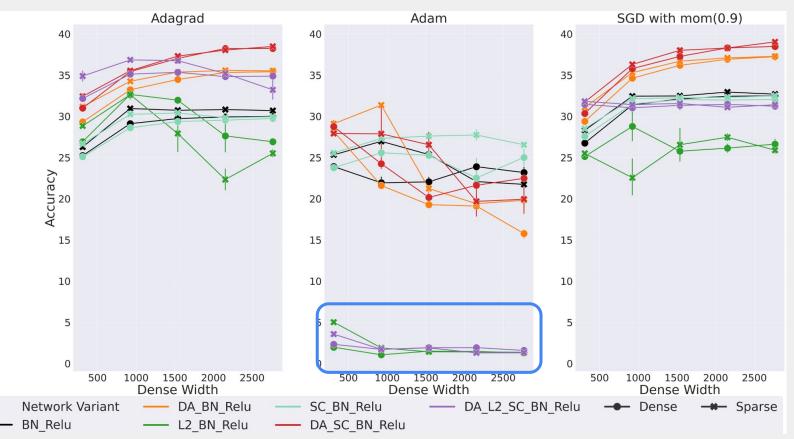
Batch Norm Stabilizes Grad Flow - Gradient Flow - 4hl



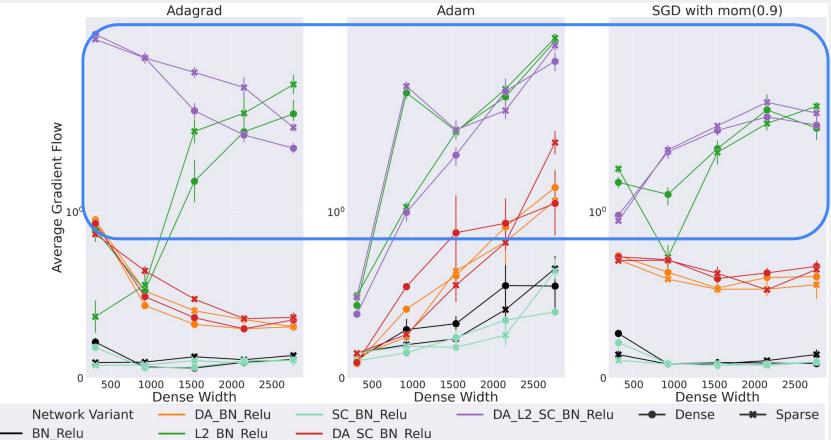
Batch Norm



2. EWMA Optimizers Are Sensitive to High Gradient Flow Accuracy



2. EWMA Optimizers Are Sensitive to High Gradient Flow Gradient Flow





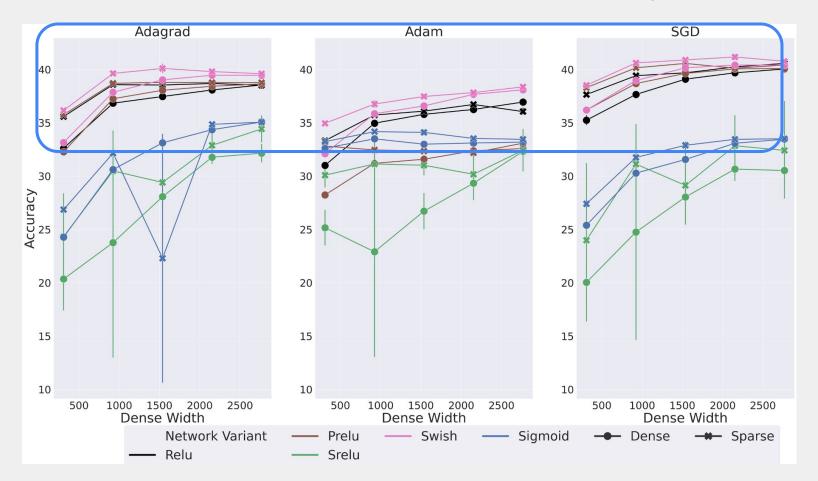
3. Activation Functions

	ReLU	Swish	PReLU	SReLU	Sigmoid	ELU
Adagrad	0.023	0.005	0.050	0.182	0.568	0.003
Adam	0.191	0.182	0.039	0.062	0.005	0.000
RMSProp	0.894	0.167	0.002	0.012	0.997	0.153
SGD	0.013	0.027	0.005	0.078	0.030	0.056
Mom (0.9)	0.212	0.013	0.001	0.078	0.001	0.973

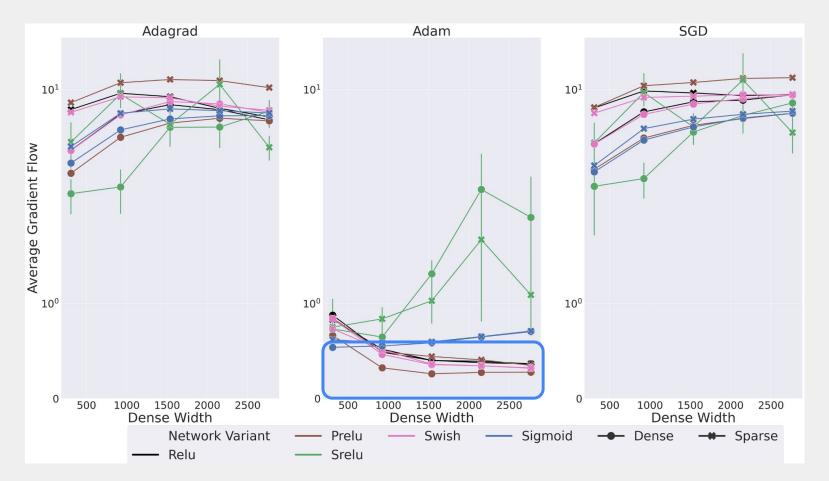


NR - No Regularization, BN - Batchnorm, SC - Skip Connections, DA - Data Augmentation, L2- weight decay, D - Dense Networks and S - Sparse Networks.

Activation Functions - Accuracy

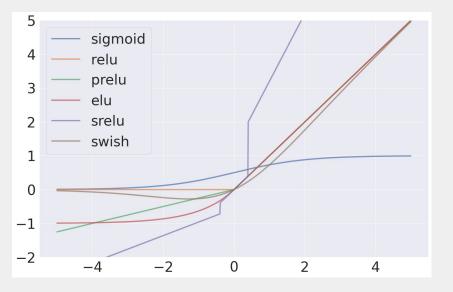


Activation Functions - Gradient Flow

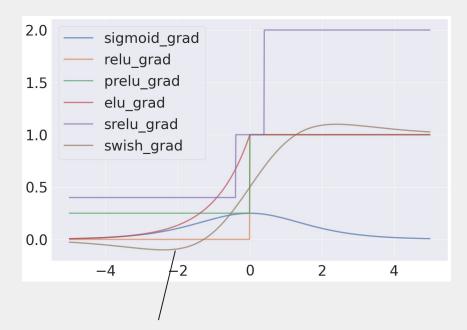


Activation Functions





b) Derivative of Activation Function with inputs [-5,5]



Allows flow of negative gradients.

Extension of Results

- Generalization of Results Across Architecture Types Wide ResNet-50.
- Generalization of Results From Random Pruning to Magnitude Pruning.

Questions???

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Tessera, Sara Hooker, Benjamin Rosman

https://arxiv.org/abs/2102.01670

Key Takeaways:

- Need better toolbox for sparse network analysis - SC-SDC and EGF.
- BatchNorm is useful for stabilizing grad flow - especially for sparse networks.
- Move away from maximizing grad flow -> stabilizing gradient flow.
- Careful choice of optims and activation functions can benefit sparse networks.

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